



# VIVEK TUTORIALS

Preliminary Examination

Std: SSC (E.M)

Subject: Mathematics II

Time: 2 Hours

Date : 23/Jan/2020

Max Marks: 40

- (i) All questions are compulsory.
- (ii) Use of calculator is not allowed.
- (iii) Total marks are shown on the right side of the question.

**Q.1 (A) Choose the correct alternative:**

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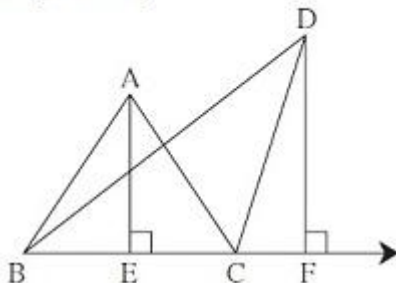
- (1)  $\triangle ABC$  is such that  $AB = 3$  cm,  $BC = 2$  cm and  $CA = 2.5$  cm. If  $\triangle DEF \sim \triangle ABC$  and  $EF = 4$  cm, then perimeter of  $\triangle DEF$  is  
(a) 7.5 cm (b) 15 cm (c) 22.5 cm (d) 30 cm
- (2) Tangents drawn from two ends of a diameter are \_\_\_\_\_.  
(a) parallel (b) intersecting (c) non-planer (d) skew
- (3) If the area of a sector of a circle is  $\frac{5}{18}$  of the area of the circle, then the sector angle is equal to  
(a)  $60^\circ$  (b)  $90^\circ$  (c)  $100^\circ$  (d)  $120^\circ$
- (4) Distance of point  $(-3, 4)$  from the origin is \_\_\_\_\_.  
(A) 7 (B) 1 (C) 5 (D) -5

**(B) Solve the following:**

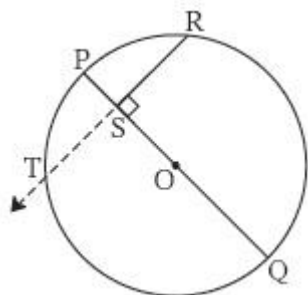
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- (1) In below figure  $AE \perp$  seg BC, seg  $DF \perp$  line BC,  $AE = 4$ ,  $DF = 6$ , then find

$$\frac{A(\triangle ABC)}{A(\triangle DBC)}$$



- (2) In figure below, seg PQ is a diameter of a circle with centre O. R is any point on the circle. seg  $RS \perp$  seg PQ. Prove that, SR is the geometric mean of PS and SQ. [That is,  $SR^2 = PS \times SQ$ ]



- (3) Prove the following:  $\tan^4 \theta + \tan^2 \theta = \sec^4 \theta - \sec^2 \theta$
- (4) Find the distance between each of the following pairs of points:  $T(-3, 6)$ ,  $R(9, -10)$

**Q.2 (A) Complete the following activities: (Any TWO)**

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- (1) Find the coordinates of point P if P divides the line segment joining the points  $A(-1, 7)$  and  $B(4, -3)$  in the ratio 2 : 3.

P(x, y) divides seg AB in the ratio 2 : 3.

A(-1, 7) = (x<sub>1</sub>, y<sub>1</sub>)

B(4, -3) = (x<sub>2</sub>, y<sub>2</sub>)

m : n = 2 : 3

By section formula,

$$x = \frac{mx_2 + nx_1}{m+n}; \text{ and } y = \frac{my_2 + ny_1}{m+n}$$

$$= \frac{2 \times 4 + 3 \times (-1)}{2+3} \text{ and } \frac{2 \times \boxed{\phantom{00}} + 3 \times (7)}{2+\boxed{\phantom{00}}}$$

$$= \frac{8-3}{5} \text{ and } \frac{-6+\boxed{\phantom{00}}}{5}$$

$$= \frac{5}{5} \text{ and } \boxed{\phantom{00}}$$

x = 1 and y = 3

∴ The coordinates of point P are (1, 3).

- (2) Measure of an arc of a circle is 80 cm and its radius is 18 cm. Find the length of the arc. ( $\pi = 3.14$ )

For a sector, r = 18 cm,  $\theta = 80$

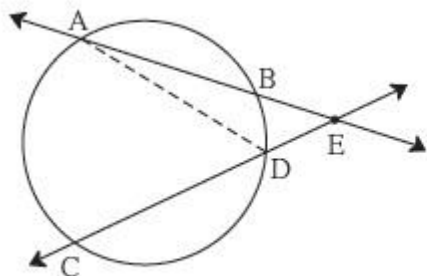
Length of an arc =  $\boxed{\phantom{00}} \times 2\pi r$

$$= \boxed{\phantom{00}} \times 2 \times 3.14 \times \boxed{\phantom{00}}$$

$$= 3.14 \times 8$$

$$= \boxed{\phantom{00}}$$

- (3) Prove that, if two lines containing chords of a circle intersect each other outside the circle, then the measure of angle between them is half the difference in measures of the arcs intercepted by the angle.



**Given :** Chords AB and CD intersect at  $\boxed{\phantom{00}}$  in the  $\boxed{\phantom{00}}$  of the circle.

**To prove:**  $\angle \boxed{\phantom{00}} = \frac{1}{2} [m(\text{arc AC}) - m(\boxed{\phantom{00}})]$

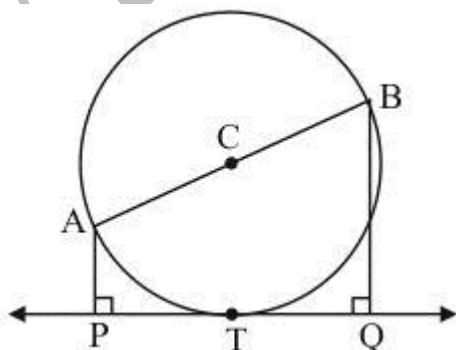
**Construction:** Draw seg AD.

Consider angles of  $\triangle AED$  and its exterior angle and write the proof.

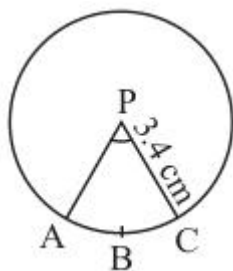
**(B) Solve the following: (Any FOUR)**

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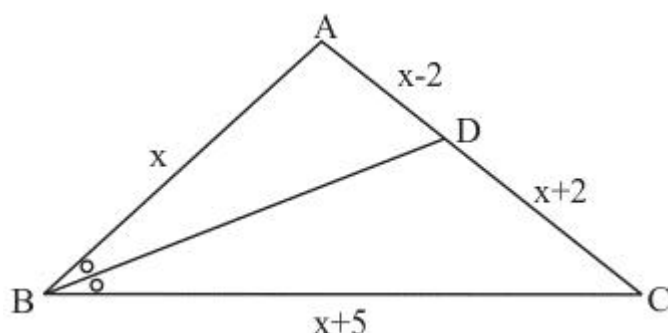
- (1) Draw any circle. Take any point A on it and construct tangent at A without using the centre of the circle.
- (2) In figure below, seg AB is a diameter of a circle with centre C. Line PQ is a tangent, which touches the circle at point T. seg AP  $\perp$  line PQ and seg BQ  $\perp$  line PQ. Prove that, seg CP  $\cong$  seg CQ.



- (3) In figure below, radius of circle is 3.4 cm and perimeter of sector P – ABC is 12.8 cm. Find A(P – ABC)

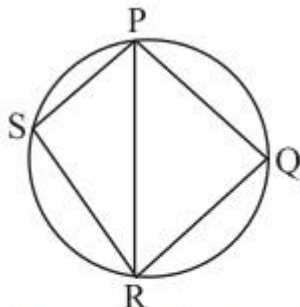


- (4) A metal parallelopiped of measures 16 cm x 11cm x 10 cm was melted to make coins. How many coins were made if the thickness and diameter of each coin was 2 mm and 2 cm respectively?
- (5) In  $\triangle ABC$ , seg BD bisects  $\angle ABC$ . If  $AB = x$ ,  $BC = x + 5$ ,  $AD = x - 2$ ,  $DC = x + 2$ , then find the value of  $x$ .



**Q.3(A) Complete the following activity:(Any ONE)**

- (1) In figure below,  $\square PQRS$  is cyclic. Side  $PQ \cong$  side  $RQ$ .  $\angle PSR = 110^\circ$ , Find-



- (1) measure of  $\angle PQR$
- (2)  $m(\text{arc } PQR)$
- (3)  $m(\text{arc } QR)$
- (4) measure of  $\angle PRQ$

□ PQRS is a cyclic quadrilateral [Given]

$$\therefore \angle PQR + \angle PSR = 180^\circ$$

[Opposite angles of cyclic quadrilateral are supplementary]

$$\therefore \angle PQR + 110^\circ = 180^\circ$$

$$\therefore \angle PQR = 180^\circ - 110^\circ = \boxed{\phantom{00}} \dots\dots 1$$

$$\angle PSR = \frac{1}{2} m(\text{arc PQR})$$

[Inscribed angle theorem]

$$\therefore 110^\circ = \frac{1}{2} m(\text{arc PQR})$$

$$\therefore m(\text{arc PQR}) = \boxed{\phantom{00}} \dots\dots 2$$

In  $\triangle PQR$ , side  $PQ \cong$  side  $RQ$  [Given]

$$\therefore \angle PQR \cong \angle QPR$$

$\dots\dots 3$  [Isosceles triangle theorem]

In  $\triangle PQR$ ,

$$\angle PQR + \angle PRQ + \angle QPR = 180^\circ$$

[Sum of all angles of a triangle is  $180^\circ$ ]

$$\therefore 70^\circ + \angle QPR + \angle QPR = 180^\circ \text{ [From 1 \& 2]}$$

$$\therefore 2\angle QPR = 180^\circ - 70^\circ$$

$$\therefore 2\angle QPR = \boxed{\phantom{00}}$$

$$\therefore \angle QPR = \boxed{\phantom{00}} \dots\dots 4$$

$$\angle QPR = \frac{1}{2} m(\text{arc QR})$$

$$\therefore 55^\circ = \frac{1}{2} m(\text{arc QR}) \text{ [From 3]}$$

$$\therefore m(\text{arc QR}) = 110^\circ$$

$$\angle PRQ = \boxed{\phantom{00}} \text{ [From 3 \& 4]}$$

(2) Determine whether the following points are collinear: A(-4,4), K(-2, 5/2), N(4, -2)

$$A(-4, 4) = (x_1, y_1)$$

$$K(-2, \frac{5}{2}) = (x_2, y_2)$$

$$N(4, -2) = (x_3, y_3)$$

$$\begin{aligned} \text{Slope of line AK} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{\frac{5}{2} - 4}{-2 - (-4)} \\ &= \left( \frac{\quad}{2} \right) \div (\quad) \\ &= \frac{-3}{2} \div 2 \\ &= \frac{-3}{2} \times \quad \end{aligned}$$

$$\therefore \text{Slope of line AK} = \quad \dots (i)$$

$$\begin{aligned} \text{Slope of line AN} &= \frac{y_3 - y_1}{x_3 - x_1} \\ &= \frac{-2 - 4}{4 - (-4)} \\ &= \frac{-6}{4 + 4} \\ &= \frac{\quad}{\quad} \\ \therefore \text{Slope of line AN} &= \frac{-3}{4} \dots (ii) \end{aligned}$$

$$\therefore \text{Slope of line AK} = \text{Slope of line } \quad \dots [\text{From (i) and (ii)}]$$

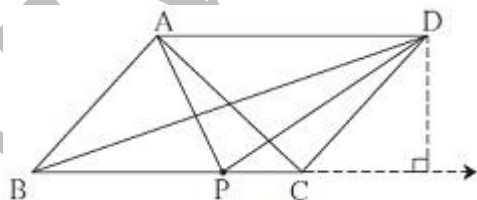
Also, they have a common point A.

$\therefore$  Point A, K and N are collinear points.

**(B) Solve the following: (Any TWO)**

6

- (1) A kite is flying at a height of 60 m above the ground. The string attached to the kite is tied at the ground. It makes an angle of  $60^\circ$  with the ground. Assuming that the string is straight, find the length of the string. ( $\sqrt{3} = 1.73$ )
- (2) ABCD is a parallelogram. P is any point on side BC. Find two pairs of triangles with equal areas.



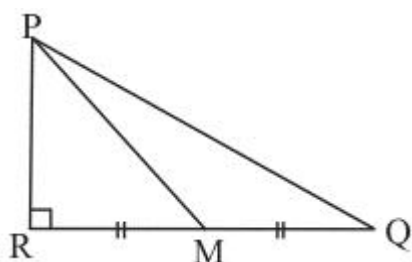
- (3) How many solid cylinders of radius 10 cm and height 6 cm can be made by melting a solid sphere of radius 30 cm?
- (4) Pranali and Prasad started walking to the East and to the North respectively, from the same point and at the same speed. After 2 hours distance between them was  $15\sqrt{2}$  km. Find their speed per hour.

**Q.4 Solve the following: (Any TWO)**

8

- (1) In  $\Delta PQR$ ,  $\angle Q = 90^\circ$ , seg QM is median.  $PQ^2 + QR^2 = 169$ . Draw a circumcircle of  $\Delta PQR$ .

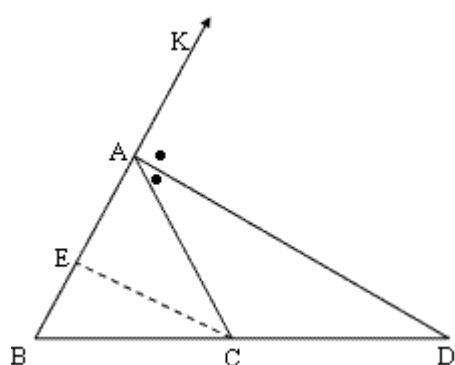
- (2) Draw a circle of radius 3.4 cm and centre E. Take a point F on the circle. Take another point A such that E-F-A and FA = 4.1 cm. Draw tangents to the circle from point A.
- (3) In the figure below, M is the midpoint of QR.  $\angle PRQ = 90^\circ$ . Prove that,  $PQ^2 = 4PM^2 - 3PR^2$ .



**Q.5 Solve the following: (Any ONE)**

- (1) In the following figure, AD is the bisector of the exterior  $\angle A$  of  $\triangle ABC$ . Seg AD intersects the side BC produced in D. Prove that:

$$\frac{BD}{CD} = \frac{AB}{AC}$$



- (2) Prove that  $(1 + \tan \theta)^2 + (1 + \cot \theta)^2 = (\sec \theta + \operatorname{cosec} \theta)^2$ .

----- All the Best -----